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Anomalous Hall effect in weak-itinerant ferrimagnet FeCr₂Te₄

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We carried out a comprehensive study of electronic transport, thermal and thermodynamic properties in FeCr₂Te₄ single crystals. It exhibits bad-metallic behavior and anomalous Hall effect (AHE) below a weak-itinerant paramagentic-to-ferrimagnetic transition $T_c \sim 123$ K. The linear scaling between the anomalous Hall resistivity ρ_{xy} and the longitudinal resistivity ρ_{xx} implies that the AHE in FeCr₂Te₄ is most likely dominated by extrinsic skew-scattering mechanism rather than intrinsic KL or extrinsic side-jump mechanism, which is supported by our Berry phase calculations.

INTRODUCTION

The anomalous Hall effect (AHE) in metals is linked to an asymmetry in carrier paths and the effects of spinorbit interaction. This is typically observed in ferromagnets since an electric current induces a transverse voltage drop in zero magnetic field which is proportional to magnetization [1, 2]. Spin-orbit coupling in the ferromagnetic bands leads to anomalous carrier velocities and intrinsic AHE [3]. The intrinsic Kaplus-Luttinger (KL) mechanism can be reinterpreted as a manifestation of Berryphase effects on occupied electronic Bloch states [4, 5]. The extrinsic mechanisms involving skew-scattering and side-jump mechanisms can also give rise to the AHE and are induced by asymmetric scattering of conduction electrons [6, 7]. In recent years it has been shown that the AHE velocities arise from the topological Berry curvature which generate an effective magnetic field in momentum space in varieties of Dirac materials with noncollinear spin configuration [8–12].

FeCr₂Ch₄ (Ch = O, S, Se, Te) materials show rich correlated electron physics. FeCr₂O₄ spinel shows a complex magnetic phase diagram with a ferrimagnetic (FIM) and multiferroic order below 80 K, a strong spin-lattice coupling and orbital order due to the Jahn-Teller distortion [13–17]. FeCr₂S₄ is a multiferroic ferrimagnet below $T_c = 165$ K with large changes of resistivity in magnetic field [18–22]. FeCr₂Se₄ orders antiferromagnetically with $T_N = 218$ K in an insulating state despite with larger ligand chalcogen atom [23–25]. FeCr₂S₄ and FeCr₂Se₄ have similar electronic structure with nearly trivalent Cr³⁺ and divalent Fe²⁺ states, and there is a strong hybridization between Fe 3d- and Ch p-states [26]. FeCr₂Te₄ shows no semiconducting gap and a FIM order below $T_c = 123$ K [27, 28].

In this work, we performed a comprehensive study of electronic and thermal transport properties in $FeCr_2Te_4$ single crystals. The AHE observed below T_c is dominated by the skew-scattering mechanism, i.e., by the Bloch state transport lifetime arising from electron scattering

by impurities or defects in the presence of spin-orbit effects, and is smaller than the intrinsic AHE revealed by density functional calculations.

EXPERIMENTAL AND COMPUTATIONAL DETAILS

Single crystals growth and crystal structure details are described in ref.[28]. Electrical and thermal transport were measured in quantum design PPMS-9. The longitudinal and Hall resistivity were measured using a standard four-probe method. In order to effectively eliminate the longitudinal resistivity contribution due to voltage probe misalignment, the Hall resistivity was obtained by the difference of transverse resistance measured at positive and negative fields, i.e., $\rho_{xy}(\mu_0 H) = [\rho(+\mu_0 H) - \rho(-\mu_0 H)]/2$. Isothermal magnetization was measured in quantum design MPMS-XL5.

We performed density functional theory (DFT) calculations with the Perdew-Burke-Ernzerhof (PBE) [29] exchange-correlation functional that is implemented in the Vienna ab initio simulation package (VASP) [30]. We adopted the experimental crystal structure with the ferrimagnetism (parallel to the lattice vector c) [28]. The cutoff energy for the plane wave basis is 300 eV. A k-mesh of $10\times10\times10$ was used in the Brillouin zone sampling. The spin-orbit coupling was included. The intrinsic anomalous Hall conductivity (AHC) and Seebeck coefficient was calculated in a tight-binding scheme based on the maximally localized Wannier functions [31].

RESULTS AND DISCUSSIONS

Figure 1(a) shows the temperature-dependent heat capacity $C_p(T)$ for FeCr₂Te₄. A clear anomaly around 123 K corresponds well to the paramagnetic (PM)-FIM transition. The high temperature $C_p(T)$ approaches the Dulong Petit value of $3NR \approx 172 \text{ J mol}^{-1} \text{ K}^{-1}$, where R

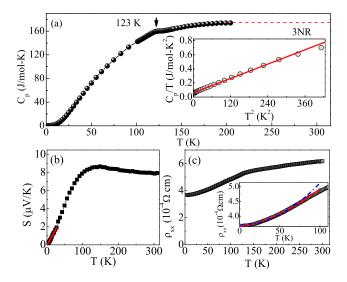


FIG. 1. (Color online) (a) Temperature-dependent heat capacity $C_p(T)$ for FeCr₂Te₄. Inset shows the low temperature $C_p(T)/T$ vs T^2 curve fitted by $C_p(T)/T = \gamma + \beta T^2$. (b) Seebeck coefficient S(T) and (c) in-plane resistivity $\rho_{xx}(T)$ for FeCr₂Te₄ single crystal. Inset in (c) shows data below 100 K fitted by $\rho(T) = \rho_0 + aT^{3/2} + bT^2$ (solid line) in comparison with $\rho(T) = \rho_0 + cT^2$ (dashed line).

= 8.314 J mol⁻¹ K⁻¹ is the molar gas constant. The low temperature data from 2 to 18 K are featureless and could be fitted by using $C_p(T)/T = \gamma + \beta T^2$, where the first term is the Sommerfeld electronic specific heat coefficient and the second term is low-temperature limit of lattice heat capacity [inset in Fig. 1(a)]. The fitting gives $\gamma = 61(2)$ mJ mol⁻¹ K⁻² and $\beta = 1.7(1)$ mJ mol⁻¹ K⁻⁴. The Debye temperature $\Theta_D = 199(1)$ K can be calculated by using $\Theta_D = (12\pi^4 NR/5\beta)^{1/3}$, where N = 7 is the number of atoms per formula unit.

The Seebeck coefficient S(T) of $\operatorname{FeCr_2Te_4}$ is positive in the whole temperature range, indicating dominant hole-type carriers [Fig. 1(b)]. The S(T) changes slope around T_c and gradually decreases with decreasing temperature. As we know, the S(T) depends sensitively on the Fermi surface. The slope change of S(T) reflects the possible reconstruction of Fermi surface passing through the PM-FIM transition. At low temperature, the diffusive Seebeck response of Fermi liquid dominates and is expected to be linear in T. In a metal with dominant single-band transport, the Seebeck coefficient could be described by the Mott relationship,

$$S = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{N(\varepsilon_F)}{n},\tag{1}$$

where $N(\varepsilon_F)$ is the density of states (DOS), ε_F is the Fermi energy, n is carrier concentration, k_B is the Boltzman constant and e is the absolute value of electronic charge [32]. The derived dS/dT below 26 K is $\sim 0.074(1)$ μ V K⁻². The S(T) curve is consistent with our calcu-

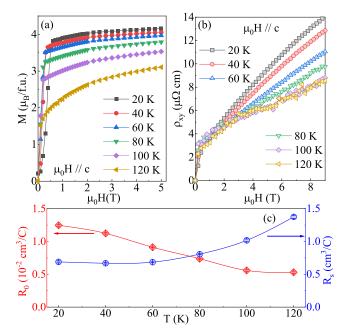


FIG. 2. (Color online) Out-of-plane field dependence of (a) dc magnetization $M(\mu_0 H)$ and (b) Hall resistivity $\rho_{xy}(\mu_0 H)$ for FeCr₂Te₄ at indicated temperatures. (c) Temperature dependence of ordinary Hall coefficient R_0 (left axis) and anomalous Hall coefficient R_s (right axis) fitted from the ρ_{xy} vs $\mu_0 H$ curves using $\rho_{xy} = R_0 \mu_0 H + R_s M$.

lations based on Boltzmann equations and DFT band structure [see below in Fig. 4(b)]. The electronic specific heat is:

$$C_e = \frac{\pi^2}{3} k_B^2 T N(\varepsilon_F). \tag{2}$$

From Eq. (1), thermopower probes the specific heat per electron: $S = C_e/ne$. The units are V K⁻¹ for S, J K⁻¹ m⁻³ for C_e , and m⁻³ for n, respectively. It is common to express $\gamma = C_e/T$ in J K⁻² mol⁻¹ units. In order to focus on the S/C_e ratio, we define a dimensionless quantity

$$q = \frac{S}{T} \frac{N_A e}{\gamma},\tag{3}$$

where N_A is the Avogadro number. This gives the number of carriers per formula unit (proportional to 1/n) [33]. The obtained q = 0.10(1) indicates about 0.1 hole per formula unit within the Boltzmann framework [33].

Figure 1(c) shows the temperature-dependent in-plane resistivity $\rho_{xx}(T)$ of FeCr₂Te₄, indicating a metallic behavior with a relatively low residual resistivity ratio [RRR = $\rho(300 \text{ K})/\rho(2 \text{ K}) = 1.7$]. A clear kink is observed at T_c , corresponding well to the PM-FIM transition. The renormalized spin fluctuation theory suggests that the electrical resistivity shows a T^2 dependence for itinerant ferromagnetic system [34]. In FeCr₂Te₄, the low temperature resistivity fitting gives a better result by adding an

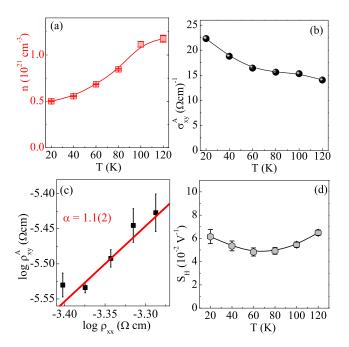


FIG. 3. (Color online) Temperature dependence of the carrier concentration (a) and the anomalous Hall conductivity $\sigma_{xy}^A = \rho_{xy}^A/(\rho_{xx}^2 + \rho_{xy}^2)$ (b). Scaling behavior of the anomalous Hall resistivity (c) and the coefficient $S_H = \mu_0 R_s/\rho_{xx}^2$ (d).

additional $T^{3/2}$ term that describes the contribution of spin fluctuation scattering [35].

$$\rho(T) = \rho_0 + aT^{\frac{3}{2}} + bT^2,\tag{4}$$

where ρ_0 is the residual resistivity, a and b are constants. The fitting yields $\rho_0 = 366(1) \,\mu\Omega$ cm, $a = 1.00(3) \times 10^{-1} \,\mu\Omega$ cm K⁻¹, and $b = 2.8(3) \times 10^{-3} \,\mu\Omega$ cm K⁻², indicating the $T^{3/2}$ term predominates. This means the interaction between conduction electrons and localized spins could not be simply treated as a small perturbation to a system of free electrons, i.e., strong electron correlation should be considered in FeCr₂Te₄.

Figure 2(a) shows the isothermal magnetization measured at various temperatures below T_c . All the $M(\mu_0 H)$ curves rapidly increase in low field and change slowly in high field. Field dependence of Hall resistivity $\rho_{xy}(\mu_0 H)$ for FeCr₂Te₄ at the corresponding temperatures are depicted in Fig. 2(b). All the $\rho_{xy}(\mu_0 H)$ curves jump in low field and then become linear-in-field in high field, indicating an AHE in FeCr₂Te₄ crystal. In general, the Hall resistivity ρ_{xy} in ferromagnets is made up of two parts,

$$\rho_{xy} = \rho_{xy}^O + \rho_{xy}^A = R_0 \mu_0 H + R_s M, \tag{5}$$

where ρ_{xy}^O and ρ_{xy}^A are the ordinary and anomalous Hall resistivity, respectively [36–39]. R_0 is the ordinary Hall coefficient from which apparent carrier concentration and type can be determined $(R_0 = 1/nq)$. R_s is the anomalous Hall coefficient. With a linear fit of $\rho_{xy}(\mu_0 H)$ in

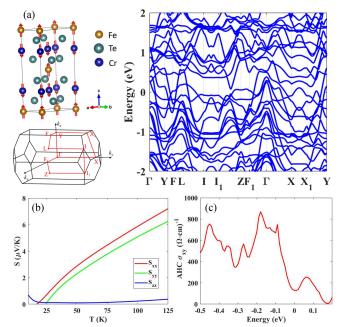


FIG. 4. (Color online) (a) Crystal structure, Brillouin zone (BZ), and electronic structure of FeCr₂Te₄. The red vectors in the crystal structure represent the directions of the magnetic moments on Fe and Cr. The high symmetric k-paths in the BZ are shown. The x, y, and z directions of the Cartesian coordinate are along the lattice vectors a, b, and c, respectively. The Fermi energy is set to zero. Calculated (b) Seebeck coefficient S and (c) anomalous Hall conductivity σ_{xy} of FeCr₂Te₄. The calculated S in low temperature shows good agreement with the experiment. The σ_{xy} at the Fermi level (zero) is \sim 127 (Ω cm)⁻¹, much larger than the measured value of 22 (Ω cm)⁻¹.

high field, the slope and intercept corresponds to R_0 and ρ_{xy}^A , respectively. R_s can be obtained from $\rho_{xy}^A = R_s M_s$ with M_s taken from linear fit of $M(\mu_0 H)$ curves in high field. The temperature dependence of derived R_0 and R_s is plotted in Fig. 2(c). The value of R_0 is positive, in line with the positive S(T), confirming the hole-type carries. The derived R_s gradually decreases with decreasing temperature. Its magnitude is about two orders larger than that of R_0 .

The derived carrier concentration n is shown in Fig. 3(a). The $n \sim 0.5 \times 10^{21}$ cm⁻³ at 20 K corresponds to ~ 0.04 holes per formula unit, comparable to the value estimated from q. Taken into account a weak temperature-dependent $\rho(T)$ [Fig. 1(c)], the estimated $n \sim 1.11 \times 10^{21}$ cm⁻³ from 484 $\mu\Omega$ cm near 100 K points to a mean free path $\lambda \sim 0.44$ nm. This is comparable to the lattice parameters and is close to the Mott-Ioffe-Regel limit [40]. The AHC σ_{xy}^A ($\approx \rho_{xy}^A/\rho_{xx}^2$) is plotted in Fig. 3(b). Theoretically, intrinsic contribution of $\sigma_{xy,in}^A$ is of the order of $e^2/(hd)$, where e is the electronic charge, h is the Plank constant, and d is the lattice parameter [41]. Taking $d \approx V^{1/3} \sim 4.3$ Å, $\sigma_{xy,in}^A$ is estimated ~ 900 (Ω cm)⁻¹,

much larger than the obtained values in Fig. 3(b). Extrinsic side-jump contribution of $\sigma_{xy,sj}^A$ is usually of the order of $e^2/(hd)(\varepsilon_{SO}/E_F)$, where ε_{SO} and E_F is spinorbital interaction energy and Fermi energy, respectively [42]. The value of ε_{SO}/E_F is generally less than 10^{-2} for metallic ferromagnets. As we can see, the σ_{xy}^A is about 22 $(\Omega \text{ cm})^{-1}$ at 20 K and exhibits a moderate temperature dependence. This value is much smaller than $\sigma_{xy,in}^A$ $\sim 900 \ (\Omega \ {\rm cm})^{-1}$, which precludes the possibility of intrinsic KL mechanism. Based on the band structure, as shown in Fig. 4, we obtained the intrinsic AHC as 127 (Ω $(cm)^{-1}$, which is much larger than the measured value too. The extrinsic side-jump mechanism, where the potential field induced by impurities contributes to the anomalous group velocity, follows a scaling behavior of $\rho_{xy}^A = \beta \rho_{xx}^2$, the same with intrinsic KL mechanism. The scaling behavior of ρ_{xy}^A vs ρ_{xx} gives $\alpha \sim 1.1(2)$ by using $\rho_{xy}^A = \beta \rho_{xx}^\alpha$ [Fig. 3(c)], which also precludes the possibility of sidejump and KL mechanism with $\alpha = 2$. It points to that the skew-scattering possibly dominates, which describes asymmetric scattering induced by impurities or defects and contributes to AHE with $\alpha = 1$. Furthermore, the scaling coefficient $S_H = \mu_0 R_s / \rho_{xx}^2 = \sigma_{xy}^A / M_s$ [Fig. 3(d)] is weakly temperature-dependent and is comparable with those in traditional itinerant ferromagnets, such as Fe and Ni $(S_H \sim 0.01 - 0.2 \text{ V}^{-1})$ [43, 44]. It is proposed that the FIM in FeCr₂Te₄ is itinerant ferromagnetism among antiferromagnetically coupled Cr-Fe-Cr trimers [28]. In a noncomplanar spin trimer structures the topologically nontrivial Berry phase is induced by spin chirality rather than spin-orbit effect, resulting in chirality-induced intrinsic AHE [45–48]. Our result excludes such scenario in Cr-Fe-Cr trimers in FeCr₂Te₄ [28].

CONCLUSIONS

In summary, we studied the electronic transport properties and AHE in $FeCr_2Te_4$ single crystal. The AHE below $T_c=123$ K is dominated by extrinsic skew-scattering mechanism rather than the intrinsic KL or extrinsic sidejump mechanism, which is confirmed by our DFT calculations. The spin structure of Cr-Fe-Cr trimers proposed for $FeCr_2Te_4$ is of interest to check by neutron scattering experiments on powder and single crystals in the future.

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